

Predictive Academic Alliances Program (PSAAP) Technical White Paper

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Predictive Science Academic Alliances Program (PSAAP) Technical White Paper

Turbulent Mixing and Hydrodynamics

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Abstract

The design of efficient, high-gain capsules for inertial confinement fusion (ICF)¹, the modeling of supernova implosions and explosions,² and the modeling of shock-induced mixing of multi-phase reactive energetic materials requires a detailed understanding of the consequences of material interpenetration, hydrodynamic instabilities and mixing at molecular (or atomic) scales arising from initial perturbations at material interfaces, i.e., the Rayleigh-Taylor, Richtmyer-Meshkov and Kelvin-Helmholtz instabilities (buoyancy-, shock- and shear-induced instabilities, respectively). From a computational point of view, this requires the development of models for hydrodynamic instability growth from initial perturbations through the weakly- and stronglynonlinear phases, and finally, to the late-time turbulent regime. In particular, modeling these processes completely and accurately is critical for demonstrating the feasibility and potential success of contemporary ICF capsule designs. In applications to energetic materials, turbulent mixing of multi-phase mixtures is a key process in anaerobic and aerobic combustion that can support shock formation and propagation. A predictive computational capability for the effects of turbulent mass, momentum, energy and species transport, as well as material mixing, on the thermonuclear fusion process in ICF entails the development of turbulent transport and mixing or subgrid-scale models based on statistically-averaged or filtered evolution equations, respectively. The former models are typically referred to as Reynolds-averaged Navier-Stokes (RANS) (and related) models³ and the latter are referred to as large-eddy simulation (LES) models.⁴ The strong nonlinearity of the equations describing the hydrodynamics, thermodynamics, material properties and other multi-scale phenomena, together with the formal ensemble averaging or filtering procedure, introduce correlations of strongly-fluctuating fields and other a priori unclosed quantities that must be explicitly modeled to close the set of equations describing the implosion dynamics and burning of an ICF capsule or the combustion of reactive materials.

Overview

The Advanced Simulation and Computing (ASC) Program is pursuing a multidisciplinary research effort to develop and quantitatively validate turbulent transport and mixing models using numerical simulations, theoretical modeling and experimental data. Specifically, it is of interest to develop state-of-the-art theoretical and numerical approaches for modeling the hydrodynamics and turbulent mixing generated by hydrodynamic instabilities induced by initial interfacial perturbations. A related objective is to establish the infrastructure needed to extract model quantities and to visualize data from large-scale direct numerical simulations (DNS)⁵ and from large-eddy or monotoneintegrated (or implicit) large-eddy simulations (MILES or ILES).⁶ Statistical information could also be extracted and applied to probability density function (PDF) or filtered density function (FDF) approaches to turbulence modeling. Numerical simulations in support of model development and *a priori* or *a posteriori* validation consider the spatiotemporal evolution of turbulent mixing⁷ induced by hydrodynamic interfacial instabilities (and possibly other types of compressible single- or multi-phase flows) on parallel computing platforms. Such data can be used to address the proper modeling of initial conditions in averaged descriptions of turbulent mixing, and to examine in detail the transition from the linear to the nonlinear and to the turbulent growth regimes. Hence, a goal is to address the physical and mathematical formulation of turbulence models, with an emphasis on the principal unclosed quantities that must be modeled using gradient diffusion and other potentially more sophisticated and physically-complete closures (e.g., second-moment closures⁸). For multi-phase flows, this requires including the effects of compressibility of all phases. Higher order closure models provide variances that are directly related to mixing properties, and which are not available from first-order closure models. Another goal is to analyze the intrinsic properties of numerical algorithms used to solve systems of equations containing either embedded turbulent transport and mixing models or explicit/implicit subgrid-scale models. It is highly desirable to relate the work above to experimental data, when available.

Presently, eddy viscosity modeling methods, LES/MILES/ILES methods, PDF/FDF and kinetic (particle) models are the methods of choice to model single- and multi-phase turbulent flows. However, the complex nonlinear physics of turbulence, as well as the proper mathematical and numerical (discrete) representation of that physics, continue to be open research areas. The ASC program is interested in research in these areas that can be applied to the computational modeling of turbulence.

Turbulent Mixing

The ASC Program requires models describing hydrodynamics and turbulence over an extensive range of spatio-temporal scales, including the development of hydrodynamic interfacial instabilities (*i.e.*, the Rayleigh-Taylor, Richtmyer-Meshkov and Kelvin-Helmholtz instabilities) from small-amplitude linear growth to weakly- and strongly-nonlinear growth, and finally to the late-time fully-developed turbulent regime. This includes the development of DNS capability and of subgrid-scale models for LES of turbulent mixing. The models should provide detailed information regarding concentration profiles, and the distribution of, and correlations among, the sizes and shapes of regions of unmixed or poorly mixed fluid. It is also necessary to develop improved constitutive closure models for the Reynolds stresses and other unclosed quantities for use in RANS or PDF/FDF models, possibly using data from DNS, LES and MILES/ILES. Research into alternatives to conventional subgrid-scale models, such as models based on filters and sub-filters, is also beneficial. Conceptual issues such as explicit filtering in complex geometries and on unstructured grids for inhomogeneous turbulence should also be addressed.

The simulations should attain very large Reynolds numbers characteristic of fully-developed turbulence and mixing. DNS resolves all of the spatial and temporal scales in the flow, whereas LES resolves only the largest scales while modeling the averaged effects of the unresolved (smaller) scales on the resolved scales. DNS is challenging, as turbulent mixing layers generated by interfacial instabilities can grow from very small-scale perturbations and a quiescent state, implying a very wide range of spatial scales. Note that conventional DNS of shock-driven flows is not possible, due to the inability to fully resolve shocks. LES is also challenging, as there is a need to model both the

subgrid-scale terms in the large-eddy equations (the explicitly or implicitly filtered conservation equations) and the unresolved initial conditions. MILES and ILES rely instead on implicit subgrid-scale models inherent in the numerical discretization of the non-dissipative fluid dynamics equations, and do not require explicit subgrid-scale models. However, such simulations do not exhibit pointwise convergence and may be ill-posed in multiple dimensions; the small scales are determined by the regularizing numerical dissipation, so that the mixing properties depend on the spatial resolution and on other properties of the algorithm. Additional research is needed in assessing the applicability of different MILES and ILES methods for simulating turbulent mixing.

Phenomenological or rigorous mathematical models are needed for the dependence of turbulent mixing properties on such conditions as the initial material density ratio at a sharp interface, the direction and history of the acceleration, the compressibility of the fluid, and the initial values of symmetry-breaking perturbations (such as initial density and velocity fluctuations, and surface roughness). These models are needed in forms suitable for numerical discretization, and it is particularly desirable that they be implemented and evaluated as RANS or subgrid-scale models within much more coarsely-zoned simulations than required to perform DNS. The models must be consistently coupled to their respective mean flow equations driving the flow.

High-fidelity turbulence modeling is of interest to predictively model unsteady, highly-nonequilibrium, inhomogeneous, anisotropic, variable-density and fully-compressible multi-phase turbulence. The transition of unstable flows to turbulence and the dependence of the mixing layer properties on the initial conditions are of interest. The development of models and codes that can incorporate the closed equations governing the Reynolds stresses and other second-order quantities, and which predict the dynamics and statistical properties of evolving hydrodynamic instabilities are sought.

Variable-density and compressibility effects¹⁰ are important in all of the applications mentioned above. In particular, it is important to understand the effects of shocks of various strengths on turbulence and on turbulent mixing layers, including the effects on coherent structures and on the structures resulting from the evolution of the instabilities through baroclinic effects within the mixing layer. Models must incorporate buoyancy, shock interactions and backscatter effects (energy transfer from small to larger scales due to nonlinear interactions).

Turbulent combustion, ¹¹ other exothermic chemical reactions and thermonuclear reactions must be incorporated and understood in the presence of all of the aforementioned phenomena. The modeling of combustion and related processes is particularly challenging, as these phenomena occur at molecular and atomic scales, which are unresolved on any possible spatio-temporal computational grid. Consequently, probabilistic descriptions ¹² have traditionally been used to model the average effects in reacting flows. The understanding of combustion and related phenomena is most useful if it spans a large range of ratios of chemical energy release to the rates of other energetic processes, such as the conversion of instability energy into turbulence and the conversion of turbulent kinetic energy into internal energy. Note that MILES and ILES methods are problematic for simulating combustion, as their inherent dissipation is likely to be insufficient to adequately model the subgrid-scale dynamics. ¹³

Whenever possible, numerical models of all of these processes should be tested and validated against high-resolution DNS or experimental data.

Hydrodynamics

The ASC Program requires the solution of a broad range of hydrodynamics problems, ranging from low-speed subsonic flows to shocked supersonic flows. The physical and mechanical phenomena of interest include turbulence and turbulent mixing of single-phase and multi-phase materials with full compressibility and material strength, high-displacement and high-strain rate flows, and highly distorted hydrodynamic flows with shocks. Three-dimensional multi-scale methods capable of modeling such phenomena over a broad range of length- and timescales and relevant dimensionless parameters are needed. Some problems of interest require the ability to track shock fronts. As the flow domains of interest can be geometrically complex, unstructured grid algorithms compatible with high-aspect ratio zoning are highly desirable.

A variety of methods have previously been used to model flows of interest, including finite-difference, finite-volume, finite-element and particle techniques. These methods can be purely Eulerian, purely Lagrangian or hybrid. Examples of hybrid methods are adaptive mesh refinement (AMR), which can model shock propagation on an Eulerian grid, and arbitrary Lagrangian-Eulerian (ALE) methods. While single-fluid flows are of interest, simulations of multi-fluid/multi-phase flows are particularly relevant.

Needed algorithm research includes: (1) determining the relative strengths, weaknesses, and domains of applicability of a wide variety of hydrodynamics algorithms (such an effort might develop test problems, some with analytic or semi-analytic solutions that can be used to evaluate algorithms); (2) evaluation of the behavior of these algorithms in codes modeling hydrodynamic flows and turbulence, transport, interphase interactions, material strength and other effects, and; (3) development of new computational fluid dynamics algorithms to improve upon deficient algorithms. For example, numerical analysis in support of turbulence and subgrid-scale model development and assessment could quantitatively analyze simulation data and apply analytical techniques (e.g., modified equation or truncation error analysis) to estimate the effects of the numerical errors and other components of an algorithm on the properties of the solutions, i.e., intrinsic numerical dissipation. Such research is essential, as the numerical algorithms used in either RANS or LES models cannot be developed independently of the models, e.g., it is important to understand the competition between the inherent numerical dissipation in the algorithm and the dissipation contributed by the turbulence model. Issues such as estimating the errors associated with a subgrid-scale model near the Nyquist scale imposed by the grid resolution and the relationship between the grid and filter scales should be addressed for the flows of interest.

It is essential to compare simulation data with a comprehensive set of hydrodynamic experiments which complement the algorithm development and evaluation. Comparisons to experimental data characterizing mixing morphologies and statistical properties of turbulent mixing would be particularly valuable.

References

- ¹Nakai, S. & Takabe, H. 1996 Principles of inertial confinement fusion—physics of implosion and the concept of inertial fusion energy. *Reports on Progress in Physics* **59** 1071–1131; Lindl, J. D. 1999 *Inertial Confinement Fusion: The Quest for Ignition and Energy Gain Using Indirect Drive*, Springer-Verlag; Atzeni, S. & Meyer-ter-Vehn, J. 2004 *The Physics of Inertial Fusion: Beam Plasma Interaction, Hydrodynamics, Hot Dense Matter*, Oxford University Press.
- ²Arnett, W. D. 1987 Supernova Theory and Supernova 1987A. *Astrophysical Journal* **319**, 136–142; Arnett, W. D., Fryxell, B. A. & Müller, E. 1989 Instabilities and Nonradial Motion in SN-1987A. *Astrophysical Journal* **341**, L63–L66; Chevalier, R. A., Blondin, J. M. & Emmering, R. T. 1992 Hydrodynamic Instabilities in Supernova Remnants: Self-Similar Driven Waves. *Astrophysical Journal* **392**, 118–130; Kimoto, P. A. & Chernoff, D. F. 1997 Radiative Instabilities in Simulations of Spherically Symmetric Supernova Blast Waves. *Astrophysical Journal* **485**, 274–284; Kane, J., Drake, R. P. & Remington, B. A. 1999 An Evaluation of the Richtmyer-Meshkov Instability in Supernova Remnant Formation. *Astrophysical Journal* **511**, 335–340.
- ³Speziale, C. G. 1998 Turbulence modeling for time-dependent RANS and VLES: A review. *AIAA Journal* **36**, 173–184; Gatski, T. B. 2004 Constitutive equations for turbulent flows. *Theoretical and Computational Fluid Dynamics* **18**, 345–369.
- ⁴Lesieur, M. & Métais, O. 1996 New Trends in Large-Eddy Simulations of Turbulence. *Annual Review of Fluid Mechanics* **28**, 45–82; Spalart, P. R. 2000 Strategies for turbulence modelling and simulations. *International Journal of Heat and Fluid Flow* **21**, 252–263; Moin P. 2002 Advances in large eddy simulation methodology for complex flows. *International Journal of Heat and Fluid Flow* **23**, 710–720; Sagaut, P. 2005 *Large Eddy Simulation for Incompressible Flows: An Introduction*, second edition, Springer-Verlag.
- ⁵Moin, P. & Mahesh, K. 1998 Direct Numerical Simulation: A Tool in Turbulence Research. *Annual Review of Fluid Mechanics* **30**, 539–578.
- ⁶Boris, J. P., Grinstein, F. F., Oran, E. S. & Kolbe, R. L. 1992 New Insights into Large Eddy Simulation. *Fluid Dynamics Research* **10**, 199–228; Hahn M. & Drikakis, D. 2005 Large eddy simulation of compressible turbulence using high-resolution methods. *International Journal for Numerical Methods in Fluids* **47**, 971–977; Margolin, L. G. & Rider, W. J. 2005 The design and construction of implicit LES models. *International Journal for Numerical Methods in Fluids* **47**, 1173–1179.
- ⁷Dimotakis, P. E. 2005 Turbulent Mixing. *Annual Review of Fluid Mechanics* **37**, 329–356.
- ⁸Speziale, C. G. 1991 Analytical Methods for the Development of Reynolds-Stress Closures in Turbulence. *Annual Review of Fluid Mechanics* **23**, 107–157; Chen, C.-J. & Jaw, S.-Y. 1998 *Fundamentals of Turbulence Modeling*, Taylor and Francis; Leschziner, M. A. 2001 Statistical Turbulence Modelling for the Computation of Physically Complex Flows. *New Trends in Turbulence*, Proceedings of the Les Houches Summer Session Vol. 74, edited by M. Lesieur, A. Yaglom and F. David, 187, Springer-Verlag.
- ⁹Drikakis, D., Grinstein, F. & Youngs, D. 2005 On the computation of instabilities and symmetry-breaking in fluid mechanics. *Progress in Aerospace Sciences* **41**, 609–641.
- ¹⁰Chassaing, P., Antonia, R. A. & Anselmet, F., Joly, L. & Sarkar, S., 2002 *Variable Density Fluid Turbulence*, Fluid Mechanics and its Applications Vol. 69, Kluwer Academic.
- ¹¹Peters, N. Turbulent Combustion, Cambridge University Press.
- ¹²Fox, R. O. 2003 Computational Models for Turbulent Reacting Flows, Cambridge University Press.
- ¹³Pitsch, H. 2006 Large-Eddy Simulation of Turbulent Combustion. *Annual Review of Fluid Mechanics* **38**,453–482.